Searching for Beyond the Standard Model Physics with COHERENT Energy and Timing Data

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Abstract

We search for beyond the Standard Model (BSM) physics by combining COHERENT energy and timing data. Focusing on light, \lesssim GeV mediators, we find the data favor a $\sim 10-1000$ MeV mediator as compared to the Standard Model (SM) best fit at the $\lesssim 2\sigma$ level. The best-fit coupling range is $g \sim 10^{-5}-10^{-3}$. The timing data provides statistical information on the neutrino flavor distributions that is not attainable from the nuclear recoil energies alone. This result accounts for uncertainty in the effective size of the neutron distribution, and highlights the power of including uncertainties on experimental backgrounds, nuclear structure, and BSM physics.

I. INTRODUCTION

The COHERENT collaboration has reported the first detection of coherent neutrinonucleus elastic scattering (CE ν NS) [1]. COHERENT utilizes the Spallation Neutrino Source (SNS) with a stopped-pion beam, which produces a well-known neutrino spectrum from pion and muon decay at rest. Muon neutrinos, ν_{μ} , arrive from prompt charged pion decay, while $\bar{\nu}_{\mu}$ and ν_{e} are produced from the delayed muon decay. With an exposure of 14.6-308 kg-days, the COHERENT collaboration identified nuclear recoil events from CE ν NS which is well in excess of the expected background events for this exposure.

The COHERENT data provides an important new channel to search for beyond the Standard Model (BSM) physics. For example, the data constrains non-standard neutrino interactions (NSI) [2, 3] due to heavy or light mediators [4–11], generalized scalar and vector neutrino interactions [12], and hidden sector models [13]. It also sets independent constraints on the effective neutron size distribution of CsI [14–16], and on sterile neutrinos [17, 18]. Low mass mediator models are particularly interesting since there are no Large Hadron Collider (LHC) constraints for mediator masses \lesssim GeV, and these models may be associated with sub-GeV dark matter [19]. The aforementioned constraints on BSM physics have mostly been extracted from the energy distribution of nuclear recoil events.

The COHERENT data do not directly identify the flavor components of the neutrino flux, though it is possible to make an estimate for the contribution of the different flavors. For example the prompt ν_{μ} component may be estimated from a timing cut, while the delayed components may be extracted from their spectral signatures. Previous authors have classified the events as prompt or delayed using a two-bin analysis in timing space [20].

In this paper we perform a likelihood analysis on the COHERENT data that utilizes the full energy and timing distributions of nuclear recoil events. These distributions provide information on the neutrino flavor components that is not available from the energy data alone, or when splitting the timing data into prompt and delayed events. We test for deviations from pure Standard Model (SM) interactions, considering as an example light mediators that couple to the SM. We show that including the timing distribution data adds substantial statistical constraining power, and favors a BSM interpretation at the $\lesssim 2\sigma$ level.

II. LIGHT MEDIATORS AND NON-STANDARD INTERACTIONS

In the SM, the differential cross section for a neutrino scattering off of a target electron or quark of mass m through a Z exchange is

$$\frac{d\sigma}{dE} = \frac{G_F^2 m}{2\pi} \left((g_v + g_a)^2 + (g_v - g_a)^2 \left(1 - \frac{E}{E_\nu} \right)^2 + (g_a^2 - g_v^2) \frac{mE}{E_\nu^2} \right) , \tag{1}$$

where G_F is the Fermi constant, E is the recoil energy, E_{ν} is the incident neutrino energy, $(g_v, g_a) = (T_3 - 2Q_{\rm em} \sin^2 \theta_W, T_3)$ are the vector and axial-vector couplings to the Z-boson, T_3 is the third component of the weak isospin, $Q_{\rm em}$ is the electromagnetic charge, and θ_W is the weak mixing angle $(T_3 = -1/2 \text{ in our convention})$. For quarks in the nucleus, if the momentum transfer between the neutrino and the nucleus is smaller than or comparable to the inverse size of the nucleus (typically $E \lesssim \mathcal{O}(50)$ MeV), coherent scattering occurs. For coherent elastic scattering off of nuclei, the axial vector contribution is proportional to the nucleus spin [21], therefore it is negligible as compared to vector contribution. The cross section for scattering on the nucleus is:

$$\frac{d\sigma}{dE} = \frac{G_F^2 Q_V^2}{2\pi} m_N \left(1 - \left(\frac{m_N E}{E_\nu^2} \right) + \left(1 - \frac{E}{E_\nu} \right)^2 \right) F(q^2) \tag{2}$$

where $F(q^2)$ is the nuclear form factor, $Q_V \equiv Z(2g_v^u + g_v^d) + N(g_v^u + 2g_v^d)$, and m_N is the nucleon mass.

The form factor is a source of uncertainty, in particular at the highest nuclear recoil energy. Since there are no direct experimental measurements of the neutron distribution in the nucleus for CsI, $F(q^2)$ may be estimated from the CE ν NS data itself. Standard parameterizations are the Helm model [22], or the symmetrized Fermi model [23]. Each of these model parametrizations are functions of the size of the neutron distribution, R_n , which can be viewed as a parameter in each model. For each of these parameterizations and including only SM contributions to the scattering rate, the best-fitting neutron radius from the COHERENT data is $R_n \simeq 5.5$ fm [14].

The SM cross-section above may be modified due to a new mediating particle which couples to neutrinos and either electrons or quarks. For example, consider a new mediator Z'_{μ} with the following interaction terms:

$$\mathcal{L} \supset Z'_{\mu}(g'_{\nu}\bar{\nu}_{L}\gamma^{\mu}\nu_{L} + g'_{f,\nu}\bar{f}\gamma^{\mu}f + g'_{f,a}\bar{f}\gamma^{\mu}\gamma^{5}f), \tag{3}$$

where g'_{ν} , $g'_{f,\nu}$, and $g'_{f,a}$ are constants associated with new physics. With this interaction we can redefine the couplings (g_{ν}, g_{a}) of Eq. (1) in the following way

$$(g_v, g_a) \Rightarrow (g_v, g_a) + \frac{g'_{\nu}(g'_{f,v}, \pm g'_{f,a})}{2\sqrt{2}G_F(g^2 + M_{Z'}^2)},$$
 (4)

where q^2 is the momentum transfer, M'_Z is the mass of the mediator, and the (-) sign applies for the case of anti-neutrino scattering.

As an extension, we can consider the case where the quarks couple to Z' via a loop containing hidden sector particles [13]. In this case a form factor parameterizes the quark coupling to the Z'. This form factor scales as q^2/Λ^2 , where Λ is the scale in the hidden sector associated with the mass of the mediator particle that generates the quark-hidden sector interactions. In this scenario, $g'_{\nu}g'_{f}$ in Eq. (4) is modified to $g'_{\nu}g'_{f}q^2/\Lambda^2$, where Λ is the mass scale of the hidden sector.

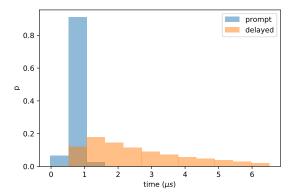
Motivated by the flavor content of the COHERENT stopped pion beam, we focus on g_e and g_{μ} , associated, respectively, with electron and muon-type neutrino couplings with the Z'. The up and down quark couplings to Z' are represented by g_u and g_d , respectively, and we will assume that $g_u = g_d = g_{\nu} = g$. Under this assumption the NSI parameter defined as $\epsilon = g'_{\nu}g'_{f,\nu}/\{2\sqrt{2}G_F(q^2 + M_{Z'}^2)\} = g^2/\{2\sqrt{2}G_F(q^2 + M_{Z'}^2)\}$ is positive, or $\epsilon = g^2q^2/\{2\sqrt{2}G_F(q^2 + M_{Z'}^2)\Lambda^2\}$ in the hidden sector scenario.

III. DATA ANALYSIS

Figure 1 shows the energy and timing distribution of COHERENT nuclear recoil events [24]. The energy distribution is given in units of photoelectrons (PEs). Our goal is to perform a joint analysis using both the timing and energy distribution to identify possible contributions from BSM physics. To represent BSM physics, we take as parameters the couplings g_e , g_{μ} , and mediator mass $M_{Z'}$. To represent the uncertainty in the nuclear structure, we take R_n as a parameter and use the Helm form factor model.

We define \mathcal{L} as the likelihood function of the model parameters given the data. We assume that the sum of the observed nuclear recoil plus background counts, $N_{obs}(t, E)$, at time t and energy E follows a Poisson model with parameter

$$\lambda(t, E) = (1 + \alpha)N(t, E, \epsilon) + N_{bg}(t, E), \tag{5}$$



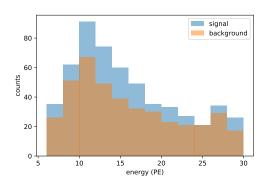


FIG. 1: Timing distribution for the prompt and delayed components (left) and energy distribution (right) as measured by COHERENT. The vertical axis in the time distribution gives the probability that an event is in a given time bin, while in the energy distribution it is the number of counts in that bin. In the energy distribution, the signal and background events are shown.

where $N(t, E, \epsilon)$ is the number of neutrino-induced nuclear recoil events predicted from the theory and $N_{bg}(t, E)$ denotes the true background count. Note that by definition $N_{bg}(t, E)$ is not observed. Rather, we have observed background counts, denoted by $N_{obs,bg}(t, E)$, that are proxy for the true background counts. We assume that given $N_{bg}(t, E)$, $N_{obs,bg}(t, E)$ follows a Poisson model with parameter $N_{bg}(t, E)$. In the absence of prior information on $N_{bg}(t, E)$, we use a non-informative prior on it, so that $\pi(N_{bg}(t, E)) \propto 1$ for $N_{bg}(t, E) \in [0, \infty)$.

In addition to the counts from the signal and the background components, Eq. (5) involves the uncertainty parameter α to account for the systematic uncertainties from flux, form factor, quenching factor, and signal acceptance uncertainties. Motivated by the results reported from COHERENT [1], we assume this parameter follows a normal distribution with zero mean and standard deviation $\sigma_{\alpha} = 0.28$. Defining $\vec{\theta} = (g_e, g_{\mu}, m, R_n)$ as the model parameters, the most general likelihood function is

$$\mathcal{L}(\vec{\theta}|t,E) \propto \prod_{(t,E)} \int \int \exp\{-\lambda(t,E)\} \frac{\{\lambda(t,E)\}^{N_{obs}(t,E)}}{N_{obs}(t,E)!} \times \frac{\exp(-\alpha^2/2\sigma_{\alpha}^2)}{\sqrt{\sigma_{\alpha}^2}}$$

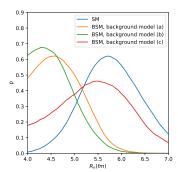
$$\times \exp\{-N_{bg}(t,E)\} \frac{\{N_{bg}(t,E)\}^{N_{obs,bg}(t,E)}}{N_{obs,bg}(t,E)!} \, \mathrm{d}\alpha \, \mathrm{d}N_{bg}(t,E). \tag{6}$$

In comparison to previous analyses, this likelihood explicitly includes information from the timing distribution. We take the bin width in energy space as the bin width in the space of the number of photoelectrons, n_e , then convert this to recoil energy space using the relation

 $n_e = 1.17(E/\text{keV})$. For the timing data we take the bin width directly from the COHERENT data, $\sim 0.5\mu\text{s}$. In the Bayesian paradigm we obtain the posterior probability densities for the model parameters using the multinest package [25] with flat prior distributions on the parameters.

To test the robustness of our modeling in light of the steady-state (SS) background observed by COHERENT, we consider three separate scenarios. In the first, which we refer to as background model (a), the SS background is fixed $(N_{bg}(t, E) = N_{bg,obs})$, and the model parameters are only $(g_e, g_\mu, M_{Z'}, R_n)$, and we do not need to integrate over the background in Eq. (6). In the second, which we refer to as background model (b), we take the background shape from the COHERENT data, but allow for an overall scaling of the background to account for an uncertainty in the normalization. For model (b) we assume that the total number of background counts follows a Poisson distribution. Instead of integrating over the background for each bin, we integrate over the total number of background counts in this scenario. In the third, which we refer to as background model (c), we take the background to be a poisson model in each bin, and integrate over the predicted number of events in each bin according to Eq. (6). For models A and B, in order to mitigate a bias in our reconstructed parameters, we exclude bins in which there are zero background counts. Using simulated data with the same number of signal and background counts as in the COHERENT data, we have verified that excluding the bins with zero background counts does not bias the reconstruction of the couplings and the mediator mass.

For comparing two models, say models 0 and 1, where one is nested within another, we use the likelihood ratio test within a frequentist paradigm. We consider the test statistic $U = -2[\log(\mathcal{L}_0) - \log\{\mathcal{L}_1(\widehat{\theta})\}]$, where we define $\log(\mathcal{L}_0)$ as the log-likelihood for model 0 in which only R_n is free and other three parameters are set to zero, and $\log\{\mathcal{L}_1(\widehat{\theta})\}$ is the log-likelihood for the model in which at least one of the parameters in $(g_e, g_\mu, M_{Z'})$ is free. For the latter model, $\widehat{\theta}$ denotes the maximum likelihood estimator (MLE) of $\overrightarrow{\theta}$, and $\widehat{\theta}$ is obtained by maximizing the marginal likelihood, Eq. (6) where $N_{bg}(t, E)$ is integrated out. The p-value of the test is $p = \operatorname{pr}(\chi_{\eta}^2 > U_{\text{obs}})$, where U_{obs} is the observed value of U and χ_{η}^2 is the chi-square distribution with η degree of freedom. Here, η is the difference between the number of estimated parameters in models 0 and 1. A small p-value provides significant evidence against the null hypothesis (SM). Applying this general procedure we can test if a model parameter (i.e., g_μ or g_e) is positive. The corresponding significance Z



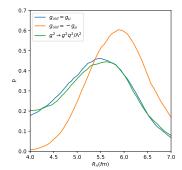


FIG. 2: Posterior probability distributions for the effective size of the nucleus, R_n , for different background models (left), for BSM models (right). The (blue) SM distribution takes R_n as a parameter, and the BSM distribution takes $(R_n, g', \text{ and } M_{Z'})$ as free parameters.

is $\Phi^{-1}(1-p/2)$, where Φ^{-1} is the inverse cumulative distribution function of the standard normal distribution. Significant results can also be seen through a large value of Z.

IV. RESULTS

We begin by considering how well R_n is determined for each of our three different background models. The posterior probability distributions for R_n are shown in the left panel of Figure 2 for each of these background models. For background models (a) and (b), the best-fit R_n is slightly lower than that from model (c), though is still statistically consistent with the result from model (c).

In order to simplify our analysis, for our BSM scenario we consider models with couplings such that $g_{\nu} = g_u = g_d = g'$. To compare the sensitivity of the data to different flavors, we either fit for g_{μ} and fix g_e , or vice versa. The key features of our analysis are unchanged if we use a different relation among the couplings.

In Figure 3, we show the resulting posterior probability distributions for g_{μ} (assuming that $g_e = 0$), for the cases of $M_{Z'} = 10$ and 1000 MeV. We show the result for background model (c), in which the background is taken to be a poisson model in each energy and time bin. The figures contain distributions using energy information alone, and distributions using both energy and timing information. For both $M_{Z'} = 10$ and 1000 MeV, the g_{μ} distributions are better constrained when including timing data, and deviate from the SM

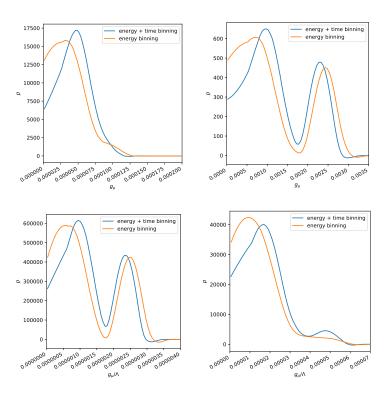


FIG. 3: Posterior probability distributions for g_{μ} (top row) or g_{μ}/Λ (bottom row, if there is form factor), using the energy data alone (orange) and using the combined energy and timing data (blue). The left column assumes a mediator mass of $M_{Z'}=10$ MeV, and the right column assumes a mediator mass of $M_{Z'}=1000$ MeV.

prediction that these couplings are zero.

We find that our results are relatively insensitive to the assumed background model. To quantify this, in Table I we show the significance Z for each of the three different background assumptions. In Table I we also show the corresponding values of Z for an analysis with the energy data alone. Here we find that statistical significance of the deviation from the SM is lower for all background models, as compared to the analysis that utilizes both energy and timing data. The results in Table I show that the timing data provides additional information on the flavor content of the fluxes that is not provided by the energy data alone. The bin-by-bin likelihood analysis that we employ is able to statistically separate the prompt and delayed distributions, with the timing information more strongly constraining the prompt g_{μ} component. In contrast, the g_e component only contributes to delayed neutrino recoil spectrum, and is less well constrained when adding in the timing information.

Figure 4 shows the probability density in $\log_{10}(M_{Z'})$ vs $\log_{10}(g_{\mu})$ or $\log_{10}(g_{\mu}/\Lambda)$ space.

Mediator mass, $M_{Z'}$ (MeV)	Fixed (model (a))	Fixed shape (model (b))	Varying (model (c))
free	1.4(0.7)	0.9(0.6)	1.1(0.6)
10	1.9(1.2)	1.4(1.1)	1.6(1.0)
100	1.9(1.1)	1.4(1.1)	1.6(1.1)
1000	1.9(1.2)	1.4(1.1)	1.6(1.1)

TABLE I: Significance in the likelihood ratio test for different background models defined in the text. The first column gives mediator mass, with the first row taking the mediator mass as a free parameter. All entries assume $g_e = 0$ and $g_{\mu} \neq 0$. Each primary entry is obtained using the combined energy and timing data, and the numbers in parenthesis use just the energy data.

The shape of the boundary in both plots can be understood as follows: in the small mediator mass region, $q^2 \gg M_{Z'}^2$, the NSI parameter is independent of the small mediator mass, while in the large mediator mass region, $M_{Z'}^2 \gg q^2$, the NSI parameter depends on $g^2/M_{Z'}^2$, thus, in log space the slope is about 1. The isolated island at large mediator mass region is because the global degeneracy for the weak charge across all energy bins (since the NSI parameter is independent of energy), thus, the constraint on the charge Q_v in Eq. (2) results in two solutions for g. On the contrary, if a hidden sector is introduced to generate a form factor $\sim q^2/\Lambda^2$, the NSI parameter becomes independent of energy in the smaller mass region and consequently, the degeneracy appears in the smaller mass region.

The above results favoring $g \neq 0$ are independent of the uncertainty in the assumed value for R_n , since we have taken R_n as a parameter in our analysis. It is however interesting to determine the manner in which R_n is degenerate with the BSM model. As an example we can compare to the case in which $g_u = g_d = -g_{\nu} = g$, as in this case there is destructive interference with the SM weak charge. The resulting R_N distribution with this assumption is shown in the right-hand panel of Fig. 2. Here we see that the degeneracy is such that larger R_N is now more favored, though the results are statistically consistent with the assumption of $g_u = g_d = g_{\nu} = g$.

To quantify the constraints on the NSI parameters in Fig. 3, we show in Table II the 1σ window of g_{μ} and g_{e} assuming 10, 100, and 1000 MeV mediator masses using our results from the energy and timing analysis. Note that this range is consistent with general constraints on the couplings and masses of light mediators [26].

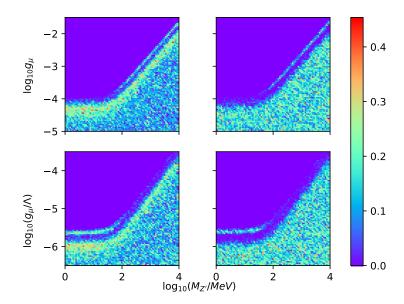


FIG. 4: Heat map of the probability density in $\log_{10}(M_{Z'})$ vs $\log_{10}g_{\mu}$ (top row) and $\log_{10}(M_{Z'})$ vs $\log_{10}(g_{\mu}/\Lambda)$ (bottom row, for a form factor q^2/Λ^2) parameter space using energy and timing data (left) and energy data alone (right).

$M_{Z'} ({ m MeV})$	10	100	1000	
g_{μ}	$1.87, 6.65] \times 10^{-5}$	$[0.41, 1.47] \times 10^{-4} \oplus [2.47, 2.66] \times 10^{-4}$	$\boxed{[0.48, 1.32] \times 10^{-3} \oplus [2.17, 2.47] \times 10^{-3}}$	
g_e	$[0, 6.12] \times 10^{-5}$	$[0, 1.53] \times 10^{-4} \oplus [2.53, 2.84] \times 10^{-4}$	$[0, 1.22] \times 10^{-3} \oplus [2.22, 2.77] \times 10^{-3}$	

TABLE II: The 1σ constraining range on g_{μ} and g_{e} using energy plus timing information.

Constraints on the NSI parameters also come from neutrino oscillation experiments. To obtain constraints from neutrino oscillation experiments, the NSI parameters are expressed as $\epsilon = g^2/\{2\sqrt{2}G_F(M_{Z'}^2)\}$. The existing constraints from the neutrino oscillation experiments are consistent with our result, within the $\sim 2\sigma$ range [4]. For example, the allowed range for a heavy mediator for $\epsilon_{\mu\mu}^u$ is [0,0.005] (our model only has positive ϵ). This converts to g = [0,0.0013] at $M_{Z'} = 1$ GeV, which covers the 1σ region as shown in Fig. 3.

There also exists so-called a LMA-Dark solution, which is characterized by larger NSI couplings and is not strongly constrained by oscillation experiments. Ref. [20] discusses this scenario specifically in the context of the COHERENT data. Since the SM is not nested within the LMA-Dark solution, to establish significance in this case we must appeal to the Bayes factor. We find that the Bayes factor is 1.12 (0.85) with (without) timing information,

which means this kind of NSI is also slightly preferred over SM if we include the timing data.

V. DISCUSSION AND CONCLUSION

We have performed a fit to the energy and timing distribution of nuclear recoil events from the COHERENT data. We have shown that including the information in both the energy and timing distributions of the COHERENT data, there is a $\sim 2\sigma$ deviation between the best-fitting model and the SM prediction. Light mediators in the mass range $\sim 10-1000$ MeV are able to provide a good fit to the data. In the appropriate limits of large mediator mass, $\gtrsim 1$ GeV, it is equivalent to a heavy mediator NSI analysis that has been performed by the COHERENT collaboration and by previous authors. This result is consistent with other experiments searching for dark photons as well as oscillation experiments.

Our analysis motivates an event-by-event analysis of COHERENT nuclear recoil events. Given information on individual nuclear recoil events, our analysis may be extended in the future by considering an unbinned limit to the likelihood, and may include appropriate uncertainty on the energy and time of an event. Future data from COHERENT [27] will better clarify the results that we have obtained.

ACKNOWLEDGMENTS

BD and LES acknowledge support from DOE Grant de-sc0010813. We acknowledge support from COS-STRP (TAMU), and would like to thank Grayson Rich and Kate Scholberg for discussions on this paper.

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